Digital Signal Processing

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Digital Signal Processing

Lecture 0

Introduction

Digital Signal Processing (DSP)

Basics:

What is DSP?

Digital Signal Processing (DSP)

Dictionary definitions of the words in DSP: • Digital

- operating by the use of discrete signals to represent data in the form of numbers
- Signal

 a variable parameter by which information is conveyed through an electronic circuit
- Processing
- to perform operations on data according to programmed instructions
 So a simple definition of DSP could be:
- changing or analysing information which is measured as discrete sequences of numbers
- Unique features of DSP as opposed to ordinary digital processing:

 signals come from the real world
 this intimate connection with the real world leads to many unique needs such as the need to react in real time and a need to measure signals and convert them to digital numbers

WHY USE DSP ?

- Versatility:
 - digital systems can be reprogrammed for other applications
 digital systems can be ported to different hardware

• Repeatability:

- digital systems can be easily duplicated
- digital systems do not depend on strict component tolerances
- digital system responses do not drift with temperature
- Simplicity:
 - some things can be done more easily digitally than with analogue systems

DSP is used in a very wide variety of applications

- Radar, sonar, telephony, audio, multimedia, communications, ultrasound, process control, digital camera, digital tv, Telecommunications, Sound & Music, Fourier Optics, X-ray Crystallography, Protein Structure & DNA, Computerized Tomography, Nuclear Magnetic Resonance: MRI,Radioastronomy
- All these applications share some common features:
 - they use a lot of maths (multiplying and adding signals) they deal with signals that come from the real world
 - they require a response in a certain time
- Where general purpose DSP processors are concerned, most applications deal with signal frequencies that are in the audio range

<sup>signals are discrete
which means the information in between discrete samples is lost</sup>





Transducers

- A "transducer" is a device that converts energy from one form to another.
- In signal processing applications, the purpose of energy conversion is to transfer information, not to transform energy.
- In physiological measurement systems, transducers may be
 input transducers (or sensors)
 - they convert a non-electrical energy into an electrical signal.for example, a microphone.
 - output transducers (or actuators)
 - they convert an electrical signal into a non-electrical energy.
 - For example, a speaker.



- Information is lost in converting from analogue to digital, due to:
 - inaccuracies in the measurement
 - uncertainty in timing
- limits on the duration of the measurement
- These effects are called quantisation errors

Analog-to Digital Conversion

- ADC consists of four steps to digitize an analog signal:
 - 1. Filtering
 - 2. Sampling
 - 3. Quantization
 - 4. Binary encoding
- Before we sample, we have to filter the signal to limit the maximum frequency of the signal as it affects the sampling rate.
- Filtering should ensure that we do not distort the signal, ie remove high frequency components that affect the signal shape.







Sampling

- Analog signal is sampled every T_s secs.
- T_s is referred to as the sampling interval.
- $f_s = 1/T_s$ is called the sampling rate or sampling frequency.
- There are 3 sampling methods:
 - Ideal an impulse at each sampling instant
 - Natural a pulse of short width with varying amplitude
 Flattop sample and hold, like natural but with single amplitude value
- The process is referred to as pulse amplitude modulation PAM and the outcome is a signal with analog (non integer) values













Sampling Theorem

$F_s \ge 2f_m$

According to the Nyquist theorem, the sampling rate must be at least 2 times the highest frequency contained in the signal.





Quantization Levels

- The midpoint of each zone is assigned a value from 0 to L-1 (resulting in L values)
- Each sample falling in a zone is then approximated to the value of the midpoint.

Quantization Zones

- Assume we have a voltage signal with amplitutes V_{min} =-20V and V_{max} =+20V.
- We want to use L=8 quantization levels.
- Zone width $\Delta = (20 -20)/8 = 5$
- The 8 zones are: -20 to -15, -15 to -10, -10 to -5, -5 to 0, 0 to +5, +5 to +10, +10 to +15, +15 to +20
- The midpoints are: -17.5, -12.5, -7.5, -2.5, 2.5, 7.5, 12.5, 17.5

Assigning Codes to Zones

- Each zone is then assigned a binary code.
- The number of bits required to encode the zones, or the number of bits per sample as it is commonly referred to, is obtained as follows:

$n_b = \log_2 L$

- Given our example, $n_b = 3$
- The 8 zone (or level) codes are therefore: 000, 001, 010, 011, 100, 101, 110, and 111
- Assigning codes to zones:
 000 will refer to zone -20 to -15
 001 to zone -15 to -10, etc.



Quantization Error

- When a signal is quantized, we introduce an error - the coded signal is an approximation of the actual amplitude value.
- The difference between actual and coded value (midpoint) is referred to as the quantization error.
- The more zones, the smaller Δ which results in smaller errors.
- BUT, the more zones the more bits required to encode the samples -> higher bit rate

Analog-to-digital Conversion

Example An 12-bit analog-to-digital converter (ADC) advertises an accuracy of \pm the least significant bit (LSB). If the input range of the ADC is 0 to 10 volts, what is the accuracy of the ADC in analog volts?

Solution: If the input range is 10 volts then the analog voltage represented by the LSB would be:

$$V_{LSB} = \frac{V_{\text{max}}}{2^{\text{Nu bits}}} = \frac{10}{2^{12}} = \frac{10}{4096} = .0024 \text{ volts}$$

Hence the accuracy would be \pm .0024 volts

Sampling related concepts

- Over/exact/under sampling
- Regular/irregular sampling
- Linear/Logarithmic sampling
- Aliasing
- Anti-aliasing filter
- Image
- Anti-image filter

Steps for digitization/reconstruction of a signal

- Band limiting (LPF)
- Sampling / Holding
- Quantization
- Coding
- These are basic steps for A/D conversion
- D/A converter
- Sampling / Holding
- Image rejection
- These are basic steps for reconstructing a sampled digital signal

Digital data: end product of A/D conversion and related concepts

- Bit: least digital information, binary 1 or 0
- Nibble: 4 bits
- Byte: 8 bits, 2 nibbles
- Word: 16 bits, 2 bytes, 4 nibbles
- Some jargon:
 - integer, signed integer, long integer, 2s complement, hexadecimal, octal, floating point, etc.



Data types

- Our first requirement is to find a way to represent information (data) in a form that is mutually comprehensible by human and machine.
 - Ultimately, we will have to develop schemes for representing all conceivable types of information language, images, actions, etc.
 - We will start by examining different ways of representing *integers*, and look for a form that suits the computer.
 - Specifically, the devices that make up a computer are switches that can be on or off, i.e. at high or low voltage. Thus they naturally provide us with two <u>symbols</u> to work with: we can call them on & off, or (more usefully) 0 and 1.

Signal

- An information variable represented by physical quantity.
- For digital systems, the variable takes on discrete values.
- Two level, or binary values are the most prevalent values in digital systems.
 - Binary values are represented abstractly by: - digits 0 and 1
 - words (symbols) False (F) and True (T)
 - words (symbols) Low (L) and High (H)
 - and words On and Off.
- Binary values are represented by values or ranges of values of physical quantities

Number Systems – Representation

- Positive radix, positional number systems
- A number with *radix* **r** is represented by a string of digits:

 $A_{n-1}A_{n-2} \dots A_1A_0 \cdot A_{-1}A_{-2} \dots A_{-m+1}A_{-m}$ in which $0 \le A_i < r$ and \cdot is the *radix point*.

• The string of digits represents the power series:

 $(\text{Number})_{r} = \left(\sum_{i=0}^{j=n-1} A_{i} \cdot r^{i}\right) + \left(\sum_{j=-m}^{j=-1} A_{j} \cdot r^{j}\right)$ (Integer Portion) + (Fraction Portion)



Unsigned Binary Integers					
Y = "abc" =	a.2	² + b.2 ¹	+ c.2 ⁰		
(where the digits a, b, c can each take on the values of 0 or 1 only)					
N = number of bits		3-bits	5-bits	8-bits	
Range is:	0	000	00000	0000000	
0 ≤ i < 2 ^N - 1	1	001	00001	00000001	
Problem: • How do we represent negative numbers?	2	010	00010	00000010	
	3	011	00011	00000011	
	4	100	00100	00000100	



Limitations of integer representations

- · Most numbers are not integer!
 - Even with integers, there are two other considerations:
- Range:
 - The magnitude of the numbers we can represent is
 - determined by how many bits we use:
 e.g. with 32 bits the largest number we can represent is about +/- 2 billion, far too small for many purposes.
- Precision:
 - The exactness with which we can specify a number:
 e.g. a 32 bit number gives us 31 bits of precision, or roughly 9 figure precision in decimal repesentation.
- We need another data type!

Real numbers

• Our decimal system handles non-integer *real* numbers by adding yet another symbol - the decimal point (.) to make a *fixed point* notation:

 $- e.g. \ 3456.78 = 3.10^3 + 4.10^2 + 5.10^1 + 6.10^0 + 7.10^{-1} + 8.10^{-2}$

- The *floating point*, or scientific, notation allows us to represent very large and very small numbers (integer or real), with as much or as little precision as needed:
 - Unit of electric charge $e = 1.602 \ 176 \ 462 \ x \ 10^{-19}$ Coulomb
 - Volume of universe = $1 \times 10^{85} \text{ cm}^3$
 - the two components of these numbers are called the mantissa and the
 exponent





IEEE-754 fp numbers - 2

Example: Find the corresponding fp representation of 25.75
 25.75 => 00011001.110 => 1.1001110 x 2⁴

- sign bit = 0 (+ve)
- normalized mantissa (fraction) = 100 1110 0000 0000 0000 0000
- biased exponent = 4 + 127 = 131 => 1000 0011
- Values represented by convention:
 - Infinity (+ and -): exponent = 255 (1111 1111) and fraction = 0
 - NaN (not a number): exponent = 255 and fraction $\neq 0$
 - Zero (0): exponent = 0 and fraction = 0
 - note: exponent = 0 => fraction is *de-normalized*, i.e no hidden 1

Binary Numbers and Binary Coding

• Flexibility of representation

- Within constraints below, can assign any binary combination (called a code word) to any data as long as data is uniquely encoded.
- Information Types
 - Numeric
 - Must represent range of data needed
 - Very desirable to represent data such that simple, straightforward computation for common arithmetic operations permitted
 - Tight relation to binary numbers
 - Non-numeric
 - Greater flexibility since arithmetic operations not applied.
 - Not tied to binary numbers

Non-numeric Binary Codes

- Given *n* binary digits (called <u>bits</u>), a <u>binary code</u> is a mapping from a set of <u>represented elements</u> to a subset of the 2^{*n*} binary numbers.
- Example: A binary code for the seven colors of the rainbow
 Code 100 is

not used

Color	Binary Number
Red	000
Orange	001
Yellow	010
Green	011
Blue	101
Indigo	110
Violet	111

