### **BLM1612 - Circuit Theory**

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First Order Circuits

**RC and RL Circuits** 

First Order Circuits

### **Objectives of Lecture**

- Explain the operation of a RC circuit in dc circuits
  - As the capacitor stores energy when voltage is first applied to the circuit or the voltage applied across the capacitor is increased during the circuit operation.
  - As the capacitor releases energy when voltage is removed from the circuit or the voltage applied across the capacitor is decreased during the circuit operation.
- · Explain the operation of a RL circuit in dc circuit As the inductor stores energy when current begins to flow in the circuit or the current flowing through the inductor is increased during the circuit operation.
  - As the inductor releases energy when current stops flowing in the circuit or the current flowing through the inductor is decreased during the circuit operation.

### **Natural Response**

- The behavior of the circuit with no external sources of excitation.
  - There is stored energy in the capacitor or inductor at time = 0 s.
  - For t > 0 s, the stored energy is released
    - · Current flows through the circuit and voltages exist across components in the circuit as the stored energy is released
    - The stored energy will decays to zero as time approaches infinite, at which point the currents and voltages in the circuit become zero.

# **RC** Circuit

- Suppose there is some charge on a capacitor at time t = 0 s.
  - This charge could have been stored because a voltage or current source had been in the circuit at t < 0 s, but was switched off at t = 0 s.
- We can use the equations relating voltage and current to determine how the charge on the capacitor is removed as a function of time.
  - The charge flows from one plate of the capacitor through the resistor  $\mathbf{R}$  to the other plate to neutralize the charge on the opposite plate of the capacitor.

















• The natural response of an inductive circuit refers to the behavior (in terms of currents) of the circuit itself, with no external sources of excitation.

- The natural response depends on the nature of the circuit alone, with no external sources.
  - In fact, the circuit has a response only because of the energy initially stored in the inductor.
- The current response of the RL circuit



### **Singularity Functions**

- Singularity functions (also called switching functions) are very useful in circuit analysis.
- They serve as good approximations to the switching signals that arise in circuits with switching operations.
- They are helpful in the neat, compact description of some circuit phenomena,
  – especially the step response of *RC* or *RL* circuits
- Singularity functions are functions that either are discontinuous or have discontinuous derivatives.











## **Relationships of singularity functions**

• The three singularity functions (impulse, step, and ramp) are related by differentiation as

$$\delta(t) = \frac{du(t)}{dt}, \qquad u(t) = \frac{dr(t)}{dt}$$

• or by integration as

$$u(t) = \int_{-\infty}^{t} \delta(\lambda) d\lambda, \qquad r(t) = \int_{-\infty}^{t} u(\lambda) d\lambda$$



- AKA a forced response to an independent source
- Capacitor and inductor store energy when there is:
  - a transition in a unit step function source, u(t-to)
  - a voltage or current source is switched into the circuit.



# **RC Circuit**

• Find the final condition of the voltage across the capacitor.









As the inductor has not stored any energy because no power source has been connected to the circuit as of yet, all voltages and currents are equal to zero.









voltages in a circuit have reached steady-state once  $5\tau$  have passed after a change has been made to the value of a current or voltage source in the circuit.

























# $\label{eq:total_states} \begin{array}{l} \mbox{...Example 03} \\ \mbox{t} > 2ms \\ & \tau = R_{eq}C = 3k\Omega(2\mu F) = 6 \mbox{ ms} \\ & V_C = V_C(2ms)e^{-(t-2ms)/\tau} = 4V \ e^{-(t-2ms)/6ms} \\ & V_R = V_C \\ & I_C = C \ dV_c/dt = 2\mu F(-4V/6ms) \ e^{-(t-2ms)/6ms} \\ & = -1.33 \ e^{-(t-2ms)/6ms} \ mA \\ & I_R = - \ I_C = 1.33 \ e^{-(t-2ms)/6ms} \ mA \\ & Note \ I_R + I_L = 0 \ mA \end{array}$









